## **Presentation Topics**

- 1. Direct image of a measure [Lang, Ch. VI, Exercises 1 and 8] & inverse image of a measure.
- 2. Convolution of measures [Lang, Ch. VI, Exercise 16].
- 3. Countable products of measure spaces [Lang, Ch. VI, Exercise 22].
- **4.** Hausdorff outer measure (of any dimension) is a metric outer measure & 0-dimensional Hausdorff measure is the counting measure [hints in Falconer, p.7].
- 5. Key Lemma + corollary on Hausdorff dimension [Lecture notes; hints in Falconer, p.7].
- **6.** A set  $X \subset \mathbb{R}^n$  is Hausdorff measurable iff X is contained in a  $G_{\delta}$ -set G with  $G \setminus X$  of measure 0 iff X contains an  $F_{\sigma}$ -set F with  $X \setminus F$  of measure 0 [cf. Falconer, Thm. 1.6].
- 7. Vitali Covering Theorem [Falconer, Thm. 1.10].
- 8. In  $\mathbb{R}^n$ , the *n*-dimensional Hausdorff measure coincides with Lebesgue measure [Falconer, Thm. 1.12].

## **References:**

- 1. S. Lang, Real and functional analysis, 3rd edition, Springer, GTM 142, 1993.
- 2. K. J. Falconer, The geometry of fractal sets, Cambridge University Press, 1985.